

LECTURE 1: INTRODUCTION TO PRINCIPLES OF FINANCE

- **Financial system** – comprised of financial institutions, instruments, markets (facilitating transactions for goods and services + financial transactions)
 - Settle commercial transactions – domestic & international
 - Arrange **flow of funds** between **surplus** & **deficit** units (through contracts)
 - Funds can flow through **intermediaries** or through **financial markets (direct financing)**
 - Transfer and manage **risk**
 - Generate information to assist **decision making**
 - Deal with incentive problems in **contracting**
 - Pooling of **funds**
- **Surplus units** – suppliers of funds
 - Lenders
 - Investors
 - Shareholders
- **Deficit units** – users of funds / using someone else's money
 - Borrowers
 - Credit card users
 - Companies/issuers
- **Intermediation (indirect financing)** – transfer of funds between ultimate savers and ultimate borrowers via deposit-taking institutions
 - **Asset transformation** – borrowers and savers are offered a range of products
 - **Maturity transformation** – borrowers and savers are offered products with a range of terms to maturity (different time periods)
 - **Credit risk diversification and transformation** – saver's credit risk limited to the intermediary (which has expertise and information)
 - You only have to worry about the bank's situation – not the person who has loaned out your deposited money
 - **Economies of scale** – financial and operational benefits of organisational size and business volume
- **Direct financing** – transfer of funds from ultimate savers to ultimate borrowers without an intermediary
 - e.g. issuing shares & raising capital directly from shareholders
 - **ADVANTAGES:**
 - Avoids costs of intermediation
 - Increases access to diverse range of markets
 - Greater flexibility in range of securities users can issue for different financing needs
 - **DISADVANTAGES:**
 - Matching of preferences
 - Liquidity and marketability of a security
 - Search and transaction costs

- **Security** – financial contract that can be traded in a financial market which specifies:
 - **Asset involved** – commodity, hard asset, financial asset
 - **Quantity and unit** – thousand shares, ounce of gold
 - **Price, date and payment + settlement terms**
- **Primary markets** – securities are issued for the first time
 - Investors purchase securities directly from the issuer
 - Direct financing raises funds in **larger amounts** because the issue of securities requires a substantial effort that is only economical for large amounts
- **Secondary markets** – the buying and selling of existing financial securities between investors
 - No new funds raised = no direct impact on original issuer of security
 - Transfer of ownership from one saver to another saver
 - Provides liquidity
 - Facilitates the restructuring of portfolios of security owners
 - It does not raise funds for issuers... greatly assists operations of primary market
 - Provides investors with liquidity
 - Transforms the maturity of funds
 - **Price discovery** – identify the price (or value) of the securities
 - Identify investors who are interested in securities (who could be approached to supply funds in the primary market)

DIFFERENT TYPES OF FIRMS

- **Limited liability companies** – separate legal entity from its owners
 - Limits owners **liability** to their investment
 - **Taxed** in its own right and can be sued in its own rights
 - Can be public (trade on an exchange) or private (banned from being traded on an exchange)
 - Usually run by professional managers (agents) on behalf of the owners – especially for public limited liability companies
 - Incentive of managers may not always be aligned with the owners!
- **Sole proprietorships** – no separation between owner and the firm
 - Unlimited **liability**
 - **Taxed** as same entity
 - Business is owned and run by one person with some employees
 - Easy to set up
 - Agency issues are not a big problem
 - Size of business limited by owner's wealth and their ability to borrow
- **Partnerships** – a sole proprietorship with multiple owners
 - All partners are liable for the debts of the business
 - Combines wealth and abilities of multiple individuals
 - Easy to setup but a new partnership will need to be formed if an existing partner sells their stake or dies

FIVE FUNDAMENTAL CONCEPTS

- Finance focuses on cash flows & is **forward-looking**
 - Identify and value the future benefits and costs of a decision
- **Law of one price** – shares (which perform the same function) have to trade at the same price
 - Assumes minimal transaction costs
- **Arbitrage** – selling and buying shares simultaneously to take advantage of different prices in different markets
 - Selling expensive share whilst buying cheap share
 - Results in instantaneous riskless profit
- **Time value of money** – a dollar received today is different in value to that received in one year's time
 - Inflation means that your **purchasing power is diminished**
- The greater the **risk** of an investment, the higher the **expected return**
 - Expected return on a risky asset = risk-free rate + risk premium
 - The greater the risk, the greater the required risk premium
- Main goal of managers is to maximise the market value of the firm (maximise shareholder wealth)
 - **Value of firm** = present value of future expected cash flows

$$\sum_{t=1}^n \frac{E(CF_t)}{(1+r)^t}$$

$E(CF_t)$ = expected cash flows received at end of period t
 n = number of periods over which cash flows are received
 r = rate of return required by investors

- **Shareholder wealth** = present value of shareholder's future expected cash flows
- **Simple interest** – the value of a cash flow is calculated without including any accrued interest to the principal
$$F_n = P_0(1 + n \times r)$$
$$P_0 = \frac{F_n}{1 + n \times r}$$
- **Compound interest (interest on interest)** – interest accrued is added to the principal and reinvested
 - Future value of a cash flow is calculated based on the principal and interest accrued
$$F_n = P_0(1 + r)^n$$
$$P_0 = \frac{F_n}{(1 + r)^n}$$

- **Effective interest rate** – the **annualised** rate that takes account of compounding within the year/period

$$i_e = \left(1 + \frac{r}{m}\right)^m - 1$$

$$i_e = e^r - 1$$

❖ **Example:** Assume the stated interest rate is 5% p.a. What is the *effective annual* interest rate if interest is paid: (a) semi-annually, (b) quarterly, (c) monthly, and (d) daily?

❖ Effective annual interest rates for different compounding intervals

❖ **Semi-Annual:** $i_e = (1 + 0.05/2)^2 - 1 = 0.0506 = 5.0625\%$

❖ **Quarterly:** $i_e = (1 + 0.05/4)^4 - 1 = 0.0509 = 5.0945\%$

❖ **Monthly:** $i_e = (1 + 0.05/12)^{12} - 1 = 0.0512 = 5.1162\%$

❖ **Daily:** $i_e = (1 + 0.05/365)^{365} - 1 = 0.05127 = 5.1267\%$

- If the interest rate is $i\%$ p. a. but the interest is paid m times a year, after n years $\$P_0$ will have the following future value:

$$S_n = P_0 \times \left(1 + \frac{r}{m}\right)^{m \times n}$$

$\frac{r}{m}$ = per period interest rate

$m \times n$ = total periods over which interest is compounded

❖ **Example:** Suppose your ancestor saved \$1,000 one hundred years ago with interest compounded monthly. What would its (future) value be today at an interest rate of (a) 5% and (b) 7% p.a?

❖ Here, $m = 12$ and $m \times n = 1200$

❖ At 5% p.a., $FV = 1000(1 + 0.05/12)^{1200} = \$146,880$

❖ At 7% p.a., $FV = 1000(1 + 0.07/12)^{1200} = \$1,074,555!$

- Present and future values of a cash flow depend on the following factors:

- **The time period (n)**

- Future value increases as n increases
- Present value decreases as n increases

- **The interest rate (r)**

- Future value increases as r increases
- Present value decreases as r increases

- **The method of computing interest**

- Future value increases as the compounding frequency increases
- Present value decreases as the compounding frequency increases

LECTURE 2: INTRODUCTION TO FINANCIAL MATHEMATICS AND DEBT

❖ **Example:** You invest \$10,000 for a five year period. What interest rate do you need to earn for the funds to double in that time period? If you invest \$10,000 at an interest rate of 10% p.a. how long will it take for these funds to triple in value?

❖ In the first case we have an *unknown* interest rate, r

$$\diamond P_0 = \$10,000, F_5 = \$20,000, n = 5$$

$$\diamond 10000(1+r)^5 = 20000$$

$$\diamond \text{So, } (1+r)^5 = 20000/10000 = 2$$

$$\diamond r = 2^{1/5} - 1 = 14.9\%$$

❖ In the second case we have an *unknown* time period, n

$$\diamond P_0 = \$10,000, F_n = \$30,000, r = 10\%$$

$$\diamond 10000(1.10)^n = 30000$$

$$\diamond \text{So, } (1.10)^n = 30000/10000 = 3.00$$

❖ Taking natural logs we have...

$$\diamond n \times \ln(1.10) = \ln(3.00)$$

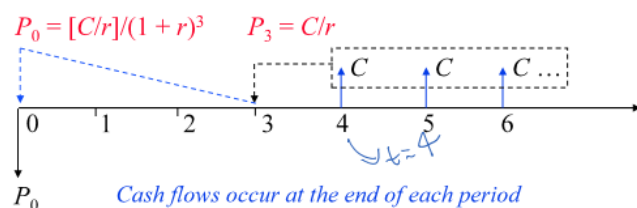
$$\diamond \text{So, } n = 1.0986/0.0953 = 11.5 \text{ years}$$

VALUING PERPETUITIES

- **Perpetuity** – equal, periodic cash flow that goes on forever

$$P_0 = \frac{C}{r}$$

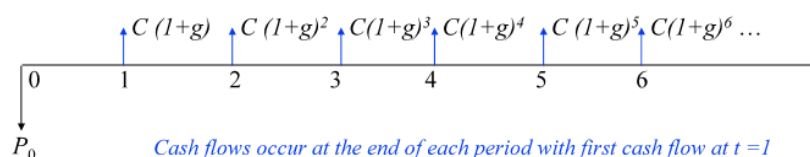
- **Deferred perpetuity** – equal, periodic cash flow that starts at some future date and then goes on forever



- Present value of a perpetuity deferred to the end of time $n + 1$

$$P_0 = \frac{C/r}{(1+r)^n}$$

- **Growth perpetuity** – perpetuity of C dollars today growing at a constant rate of g percent per period



(first cash flow assumed to be $C(1+g)$ not C)

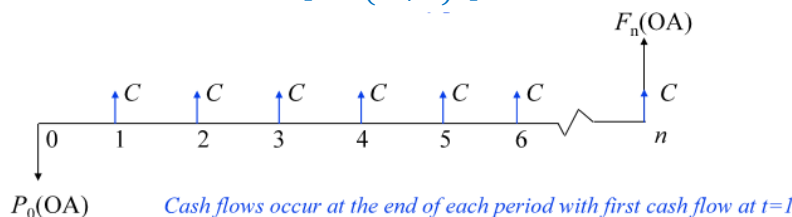
$$P_0 = C(1 + g)/(r - g)$$

- ❖ **Example:** Your company can lease a computer system for an annual lease payment of \$1,800 *now* with lease payments **increasing at a constant annual rate of 2 percent forever**, or purchase it today for \$25,000. Assume an interest rate of 10 percent per annum. Ignoring taxes and other complications, what should the company do?
- ❖ First cash flow of growth perpetuity:
 - ❖ A cash flow of \$1,800 *now* implies that $C(1 + g) = \$1,800 * 1.02 = \$1,836$ is the cash flow at $t=1$
- ❖ The present value of the lease payments is:
 - ❖ $P_0 = \$1,800 + \text{PV of Growth Perpetuity}$
 - ❖ $P_0 = \$1,800 + (\$1,800 * 1.02)/(0.10 - 0.02)$
 - ❖ Total cost = \$1,800 + \$22,950 = \$24,750.
- ❖ The company will lease the computer as less than \$25,000

VALUING ORDINARY ANNUITIES

- **Ordinary annuity** – series of equal, periodic cash flows occurring at the **end of each period** and lasting **for n periods** with **n cash flows**

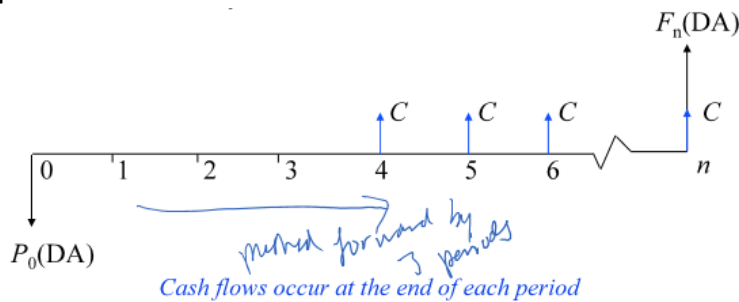
$$P_0(OA) = [C/r] \left[1 - \frac{1}{(1 + r)^n} \right]$$



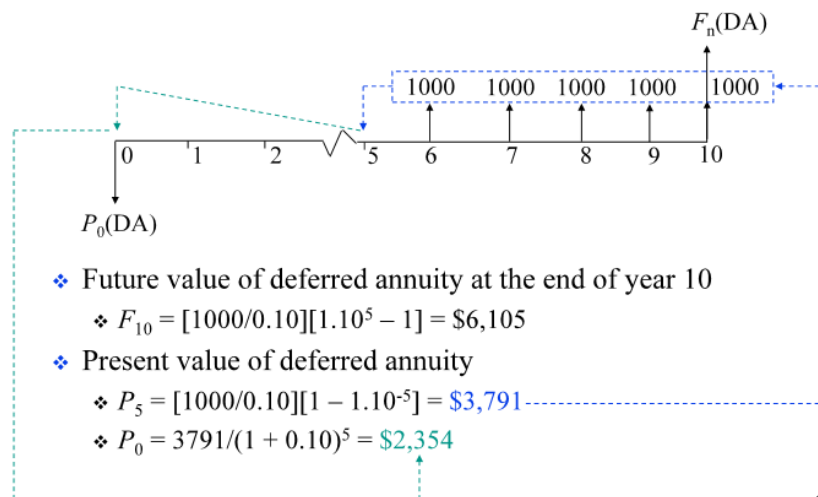
$$F_n(OA) = [C/r] \left[1 - \frac{1}{(1 + r)^n} \right] (1 + r)^n$$

- ❖ **Example:** Suppose you invest \$1,000 every year for (i) 10 years and (ii) 50 years earning an annual return of 10%.
 - a) What is each investment's value at the point where you stop investing?
 - b) What are the present values of your investments in part (a)?
 - c) What is the general relation between the future and present values calculated in parts (a) and (b)?
 - a) Future values at the end of 10 and 50 years
 - ❖ In 10 years: $F_{10} = [1000/0.10][1.10^{10} - 1] = \$15,937$
 - ❖ In 50 years: $F_{50} = [1000/0.10][1.10^{50} - 1] = \$1,163,909$
 - b) Present values of the above investments
 - ❖ Over 10 years: $P_0 = [1000/0.10][1 - 1.10^{-10}] = \$6,145$
 - ❖ Over 50 years: $P_0 = [1000/0.10][1 - 1.10^{-50}] = \$9,915$
 - c) If you had invested \$9,915 for a 50 year period, it would be worth \$1,163,909 at a 10% return p.a.
 - ❖ $9915(1.1)^{50} = \$1,163,930$ (rounding error)

- **Deferred ordinary annuity** – series of equal, periodic cash flows occurring at the **end of each period** where the first cash flow occurs at a future date

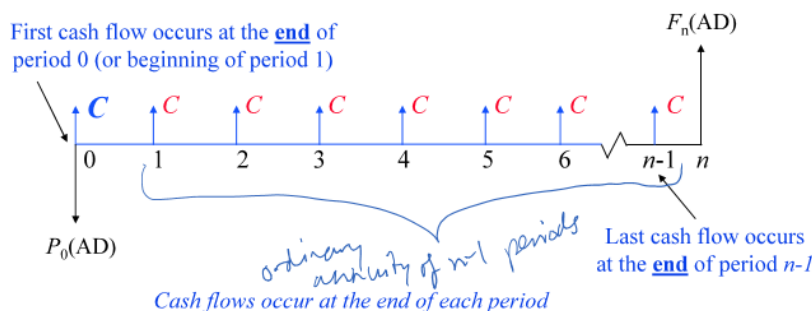


- ❖ **Example:** Suppose you plan to invest \$1,000 every year for five years and earn a return of 10% p.a. but wish to defer the investment until the end of year 6. That is, no funds are invested during years 1 - 5. What is the future value of your investment at the end of year 10 and what is the present value of your investment today?



VALUING ANNUITIES DUE

- **Annuity due** – series of equal, periodic cash flows occurring at the **beginning of each period**
 - There are **n cash flows** but only **$n - 1$ periods**
 - Effectively move annuity back one period on our standard timeline



- Present value = $P_0(OA)$ plus cash flow in year 0

$$P_0(AD) = C + [C/r] \left[1 - \frac{1}{(1+r)^{n-1}} \right]$$

$$F_{n-1}(AD) = \left\{ C + [C/r] \left[1 - \frac{1}{(1+r)^{n-1}} \right] \right\} (1+r)^{n-1}$$

- ❖ **Example:** Suppose you deposited \$1,000 every year but at the *beginning* of each year. What are the present values of these deposits earning a 10% p.a. return after (a) 10 deposits and (b) 50 deposits? What are their future values after the final deposit?

Present values of the investments are...

- ❖ Over 10 years: $P_0 = 1000 + [1000/0.10][1 - 1.10^{-9}] = \$6,759$
- ❖ Over 50 years: $P_0 = 1000 + [1000/0.10][1 - 1.10^{-49}] = \$10,906$
- ❖ Future values after 10 (at $t=9$) and 50 (at $t=49$) deposits are...
- ❖ $F_{10} = P_0[1.10^9] = \$6759 * [1.10^9] = \15937.37
- ❖ $F_{50} = P_0[1.10^{49}] = \$10906 * [1.10^{49}] = \$1,163,876.95$

APPLICATIONS

- ❖ **Application:** You have borrowed \$20,000 from your bank with the loan to be repaid in equal *annual* installments over four years. Your bank charges an annual interest rate of 10% p.a. with interest compounded annually
- What annual payment would you be making on this loan?
 - Develop a loan amortization schedule for this loan. Then using this schedule obtain the following information
 - The principal balance outstanding at the end of year 1
 - The total interest paid in year 2
 - The total principal repaid in year 3
 - The annual payments are based on the loan amount which is equal to the present value of the remaining payments
 - ❖ **Loan amount at any point = PV(Remaining payments)**
 - ❖ $20000 = \text{Payment} \times [1 - 1.10^{-4}]/0.10 = \text{Payment} \times 3.16987$
 - ❖ So, $\text{Payment} = 20000/3.16987 = \$6,309.42$
 - The loan amortization schedule shows the interest paid, principal repaid and principal remaining over the loan's duration. It can be obtained using the following:
 - ❖ **Interest paid = (Previous period's principal) \times (Interest rate)**
 - ❖ **Principal repaid = Loan Payment – Interest paid**
 - ❖ **Principal remaining = Previous period's principal – Principal repaid**

Ordinary annuity:

$$P_0(OA) = [C/r] \left[1 - \frac{1}{(1+r)^n} \right]$$

$$r = 10\%$$

$$n = 4$$

$$C = ?$$

$$P_0 = 20,000$$

Year	Annual payment	Interest paid ¹	Principal repaid ²	Principal remaining ³
0	—	—	—	\$20,000.00
1	\$6,309.42	\$2,000.00	\$4,309.42	\$15,690.58 ⁽³⁾
2	\$6,309.42	\$1,569.06 ⁽¹⁾	\$4,740.36	\$10,950.22
3	\$6,309.42	\$1,095.02	\$5,214.40 ⁽²⁾	\$5,735.82
4	\$6,309.42	\$573.58	\$5,735.84	\$0.00
Totals	\$25,237.66	\$5,237.66	\$20,000.00	

¹ Interest paid = Previous period's principal \times Interest rate

² Principal repaid = Loan Payment – Interest paid

³ Principal remaining = Previous period's principal – Principal repaid

Note: The principal outstanding at the end of year 1 can also be computed as the present value of the *remaining* payments, $P_1 = \text{Payment} \times \{[1 - 1.10^{-3}]/0.10\}$

LECTURE 3: DEBT AND EQUITY

- **Debt** – interest and principal must be paid as promised
 - Lenders rank higher than equity holders (must be paid from operational cash flows before any distribution can be made to equity holders)
- **Equity** – dividends do not have to be paid
 - Equity holders are paid last (**residual claimants**) after all other stakeholders are paid
- **Capital structure** – mix of funding sources that it uses
 - How much debt and how much equity?

DEBT SECURITIES

- **Debt security** – loan that can be traded in the (secondary) market
 - Bonds, debentures, notes, bills of exchange
 - May be issued by government and private entities
 1. Is it short-term or long-term?
 2. Does it consist of one or many future cash flows?
 3. Is it quoted and traded using simple interest or compound interest?
 - Does the issuer (borrower) have the right to repay early if they want to?
 - Is the loan secured against assets (collateral) of the borrower or unsecured?
- **Short-term debt securities**
 - Term is less than **1 year** (usually less than 6 months)
 - **Single** future cash flow
 - Quoted and traded using **simple interest**
 - **Types of short-term debt securities in Australia:**
 - Treasury notes (government debt)
 - Bills of exchange (private debt – usually guaranteed by a bank)
 - Promissory notes (private debt – not guaranteed by a bank)
 - Term of 6 months or less
 - Single payment (**face value**) on the maturity date
 - Securities are traded using simple interest on a **yield** basis in the secondary market
- **Treasury notes**

Example of primary market pricing

The government (through the Reserve Bank) issues a 13-week Treasury note. It is bought by Unisuper, a superannuation fund.

The note has a face value of \$10,000,000 and is issued at a yield of 7.650% pa.

What is the price? (That is, how much has the government borrowed?)

Answer

- ❖ The term of the note is measured precisely as the fraction of a year.
 - ❖ 13 weeks is 91 days, so the term of the note in years is $91/365$.
- ❖ The holder of the note (the lender) will be paid \$10,000,000 on the maturity date.
- ❖ The price of the note is its present value, calculated using a simple interest rate of 7.650% pa.

The formula for present value, using simple interest is:

$$P = \frac{F_n}{1 + r n}$$

Therefore:

$$\begin{aligned} P &= \frac{\$10,000,000}{1 + 0.0765 \times \frac{91}{365}} \\ &= \frac{\$10,000,000}{1.019072603} \\ &= \$9,812,844 \end{aligned}$$

$\begin{aligned} F &= 10,000,000 \\ r &= 7.650\% \\ n &= \frac{91}{365} \end{aligned}$
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Example of secondary market pricing

After holding the note for 3 weeks (21 days), Unisuper decided to sell the note in the secondary market to the Commonwealth Bank. Unisuper and the bank agreed that the note should be sold at a yield of 7.550% pa. This rate was determined by market conditions at the time.

How much will the Commonwealth Bank pay Unisuper?

Answer

We now have $r = 0.0755$ and $d = 91 - 21 = 70$ days.

F , of course, is unchanged at \$10,000,000.

$$\begin{aligned} P &= \frac{\$10,000,000}{1 + 0.0755 \left(\frac{70}{365} \right)} \\ &= \$9,857,272 \end{aligned}$$

$$P = P_0 = \frac{F}{1 + r \left(\frac{d}{365} \right)}$$

P = price

F = face value

r = required yield

d = remaining term to maturity

- **P and r are inversely related** (interest rates are always inversely related to price)
 - If required yield (r) increases, then the price (P) decreases (to make bond more attractive)
 - If required yield (r) decreases, then the price (P) increases